



# Scene Matching on Imagery

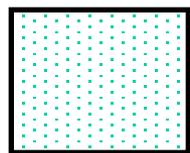
- There are a plethora of algorithms in existence for automatic scene matching, each with particular strengths and weaknesses
- SAR scenic matching for interferometry applications is difficult for several reasons:
  - Thermal noise causes the fine structure of two SAR images to differ, adding noise to the correlation measurements.
  - Geometric speckle noise is similar in images acquired in nearly the same geometry, but as the interferometric baseline increases, differing speckle noise corrupts the matching correlation.
  - Scene decorrelation is another form of speckle noise difference that corrupts matching correlation.
- SAR scenic matching for mosaicking applications involves greater challenges, including severe speckle noise differences, layover and shadow effects.



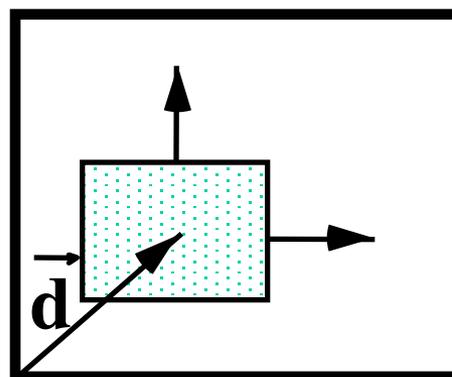
# Automatic Scene Matching

- Find overlap region and sample points at specified spacing in along track and cross track direction.
- Typical window sizes are 64x64 pixels for image data and 64x64 or 128x128 pixels for height data.
- Uses a modified Frankot's method for rejecting bad matches and to provide an estimate of the match covariance matrix.
- Cross correlation uses a normalized mean correlation function, mean of search window is calculated over the region in common with the reference window.

**Mean of reference  
is constant**



**Reference  
Window**



**Search Window**

**Mean of search  
varies with position**



# Match Correlation Estimate

- Correlation is computed in the spatial domain using a normalized cross correlation algorithm.
- Let  $I_1(\vec{x})$  be the image values at a point  $\vec{x}$  in the reference window in the first data set,  $\bar{I}_1$ , the mean of the intensities in that window.
- Let  $I_2(\vec{x} + \vec{d})$  be the image value at point  $\vec{x} + \vec{d}$  in the search window of the second data set, and  $\bar{I}_2(\vec{d})$  the mean of the intensities in that window.
- Viewing each image as a vector in an n-dimensional vector space then the cross correlation is computed as

$$c(\vec{d}) = \frac{\langle I_1 - \bar{I}_1, I_2(\vec{d}) - \bar{I}_2(\vec{d}) \rangle}{\sqrt{|I_1 - \bar{I}_1| |I_2(\vec{d}) - \bar{I}_2(\vec{d})|}} = \frac{\langle I_1 - \bar{I}_1, I_2(\vec{d}) - \bar{I}_2(\vec{d}) \rangle}{\sigma_{I_1} \sigma_{I_2(\vec{d})}}$$

where  $\sigma_{I_1}$  and  $\sigma_{I_2(\vec{d})}$  are the standard deviations of the image intensities in data sets 1 and 2, respectively.

**Space-domain correlation used for speed and because large irregular data gaps are trouble free.**



# Baseline Estimation from Offsets

- Baseline estimation in repeat pass interferometry is a rich subject, and will be covered completely in a separate module. Briefly:
- Offset field determined from scene matching carries information sufficient to reconstruct the baseline to an accuracy commensurate with ability to co-register images.
- For nearly parallel, smoothly varying, orbit tracks, the baseline can be modeled as a simple function of the range  $\rho$

$$B_{\parallel}(\rho) \approx B \sin(\theta_0(\rho) - \alpha) = \Delta\rho(\rho)$$

$$B_{\perp}(\rho) \approx B \cos(\theta_0(\rho) - \alpha) = \frac{d\Delta\rho}{d\theta}(\rho)$$

- **Solve two equations for two unknowns:  $B, \alpha$**
- **Evaluating baseline at several widely-spaced along-track (azimuth) locations gives azimuth history of the baseline.**



# Converging Baselines

- For orbit tracks with substantial convergence, azimuth offsets strongly characterize convergence rates.

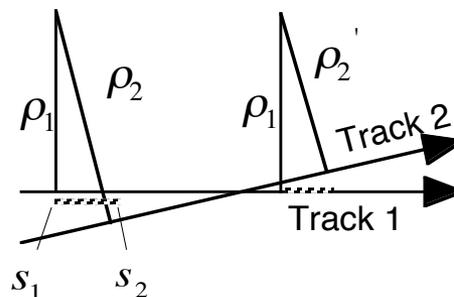
**Observation vector:**

$$\{\dots, \Delta\rho(\rho_i, a_i), \Delta a(\rho_i, a_i), \Delta\rho(\rho_{i+1}, a_{i+1}), \Delta a(\rho_{i+1}, a_{i+1}), \dots\}$$

**Parameter vector:**  $\{B_{s0}, B_{c0}, B_{h0}, \gamma, \frac{\partial B_c}{\partial s}, \frac{\partial B_h}{\partial s}\}$

where  $\gamma$  is an image scaling factor resulting from velocity differences between the tracks, and  $(s, c, h)$  are local coordinates defined by the orbit track (see notes on coordinate systems).

Slant range plane  
seen from above





# Baseline Accuracy from Offsets

- Baselines determined from offset fields are typically accurate to a fraction of the scene matching accuracy that depends on the model function and the number of offset estimates. Example:
  - Zero baseline image pair with 10 match points across range.
  - Scene matching accuracy of 1/20 pixel resolution at typical single look resolution of 15 meters:  $75 \text{ cm} / 3 = 25 \text{ cm}$
- This accuracy is insufficient for topographic mapping applications

$$\sigma_h = \frac{\rho}{B} \sin \theta \cos \alpha \sigma_{B_z}$$

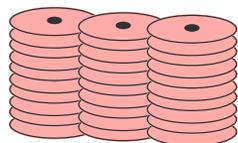
$$= 320 \text{ m} \quad ; \quad \rho = 830 \text{ km}, B = 250 \text{ m}, \theta = 23^\circ, \alpha = 0, \sigma_{B_z} = 25 \text{ cm}$$

**These geometric parameters are typical of ERS with baselines suitable for topography. Generally, ground control points tied to the unwrapped interferometric phase are required for mapping.**



# Interferogram Formation

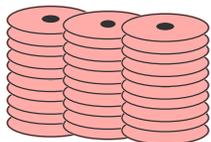
Track 1



Independently  
Processed  
Single Look  
Complex Images

Doppler spectra  
matched during  
processing

Track 2



Resample  
Complex Image

Corregistration Offset  
Estimates

2-D Polynomial  
Fit

Cross-  
Multiply and  
Multilook

Interferogram



Detected Imagery



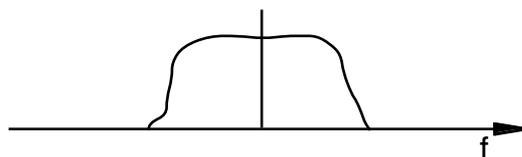
From interferogram and  
detected imagery, corr-  
lation can be formed  
properly at any resolution:  
*i.e. average of correlation  
is not correlation of average*



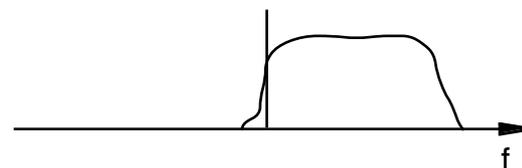
# Registration Implementation

- In resampling single look complex image to register properly with the reference image, care must be taken in interpolation of complex data
  - The azimuth spectrum of squinted SAR data is centered at the Doppler centroid frequency - a band-pass signal
  - Simple interpolators, such as linear or quadratic interpolators, are low-pass filters and can destroy band-pass data characteristics
- Band-pass interpolators or spectral methods preserve phase fidelity

SIGNAL SPECTRUM (1-D)



LOW PASS SIGNAL

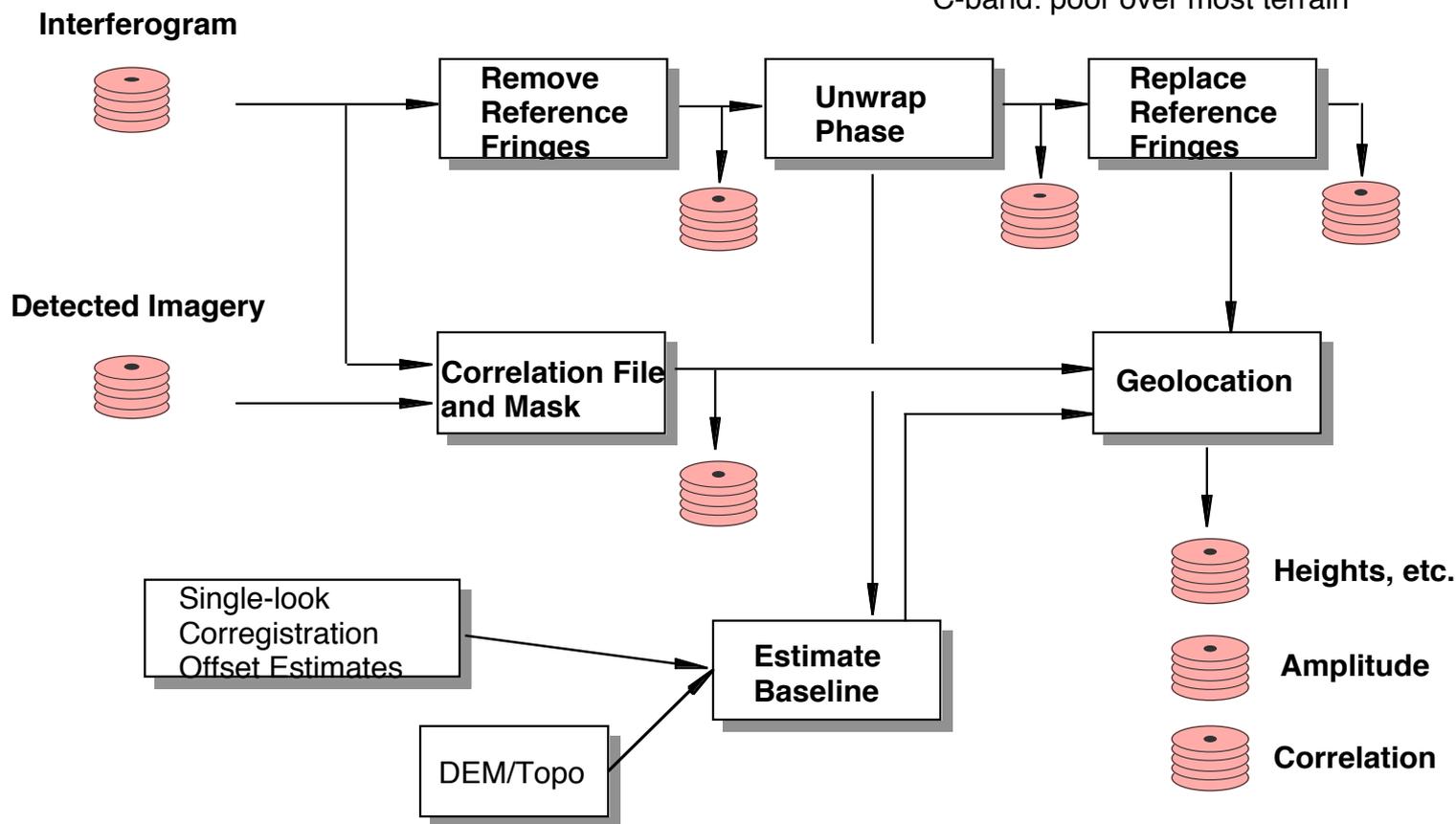


BAND PASS SIGNAL



# Repeat Pass Interferometry Back-end Processing

Performance Summary:  
L-band: good over most terrain  
C-band: poor over most terrain





# N-pass Differential Processing

